

LIMITI DI FUNZIONI IN DUE VARIABILI

Calcolare i seguenti limiti o dimostrare che non esistono:

$$1) \lim_{(x,y) \rightarrow (0,0)} \frac{x^2 y^2}{x^4 + y^2}$$

$$2) \lim_{(x,y) \rightarrow (0,0)} \frac{x^3 y}{x^4 + y^2}$$

$$3) \lim_{(x,y) \rightarrow (0,0)} \frac{x^2 y}{x^4 + y^2}$$

$$4) \lim_{(x,y) \rightarrow (0,0)} \frac{x^3 y}{x^6 + y^6}$$

$$5) \lim_{(x,y) \rightarrow (0,0)} \frac{x^4 + y^3}{x^2 + y^2}$$

$$6) \lim_{(x,y) \rightarrow (0,0)} \frac{x^2 + y^2}{x^6 + y^6}$$

$$7) \lim_{(x,y) \rightarrow (0,0)} \frac{x^{100} y^{100}}{x^2 + y^2}$$

$$8) \lim_{(x,y) \rightarrow (0,0)} \frac{x^{100} y^{100}}{x + y}$$

$$9) \lim_{(x,y) \rightarrow (0,0)} \frac{x^5 y^2}{x^6 + y^8}$$

$$10) \lim_{(x,y) \rightarrow (0,0)} \frac{x^2 y^5}{x^6 + y^8}$$

$$11) \lim_{(x,y) \rightarrow (0,0)} \frac{x^3 y^4 + x^5 + y^5}{x^4 + y^4 + x^6 y^3}$$

$$12) \lim_{(x,y) \rightarrow (0,0)} \frac{x^3 y^4}{x^6 + y^6}$$

$$13) \lim_{(x,y) \rightarrow (0,0)} \frac{x^2 y^7}{x^8 + y^8}$$

$$14) \lim_{(x,y) \rightarrow (0,0)} \frac{x^4 + y^2}{x^2 + y^4}$$

$$15) \lim_{(x,y) \rightarrow (0,0)} \frac{x^4 + y^4 + x^3 y^3}{x^8 + y^8 + x^9 - y^9}$$

$$16) \lim_{(x,y) \rightarrow (0,0)} \frac{x^4 + y^4 + x^3 y^3}{x^8 + y^8 + x^6 - y^6}$$

$$17) \lim_{(x,y) \rightarrow (0,0)} \frac{x^4 + y^4}{x^2 + y^2 + xy}$$

$$18) \lim_{(x,y) \rightarrow (0,0)} \frac{x^4 + y^4}{x^2 + y^2 + 2xy}$$

$$19) \lim_{(x,y) \rightarrow (0,0)} \frac{x^9 y^8}{(x^8 + y^{20})(x^{10} + y^8)}$$

$$20) \lim_{(x,y) \rightarrow (0,0)} \frac{2x^2 + 3y^2 + x^4}{x^2 + 8y^2 + x^6 - y^6}$$

$$21) \text{ Studiare, al variare di } \alpha \geq 0 \text{ il } \lim_{(x,y) \rightarrow (0,0)} \frac{x^\alpha y^3}{(x^{30} + y^{18})(x^{10} + y^{10})}$$